

TUE-PM-320

# Two-way Multi-Label Loss

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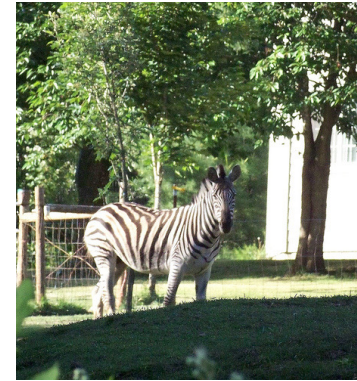
*University of Tsukuba*

# Image Classification

- Real images frequently contain multiple targets.
- It poses **multi-label classification**, in comparison to a standard single-label one, e.g., ImageNet.



- ✓ zebra
- ✓ giraffe
- ✓ car
- ✓ truck



- ✓ zebra

Task:

**Multi-label classification**

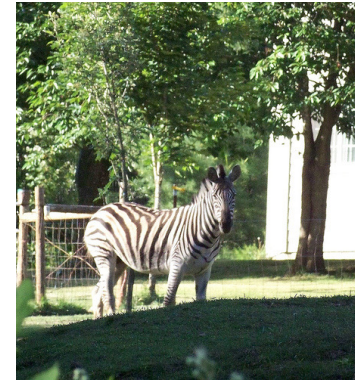
Single-label classification

# Gap between Softmax and Multi-Label

- Although **softmax loss** works quite well in single-label scenario, it is rarely applied to multi-label learning.
  - There is a gap between the softmax loss and multi-label classification.



- ✓ zebra
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- ✓ zebra

Task:

**Multi-label classification**

Single-label classification

Loss:

BCE loss

**Softmax loss**

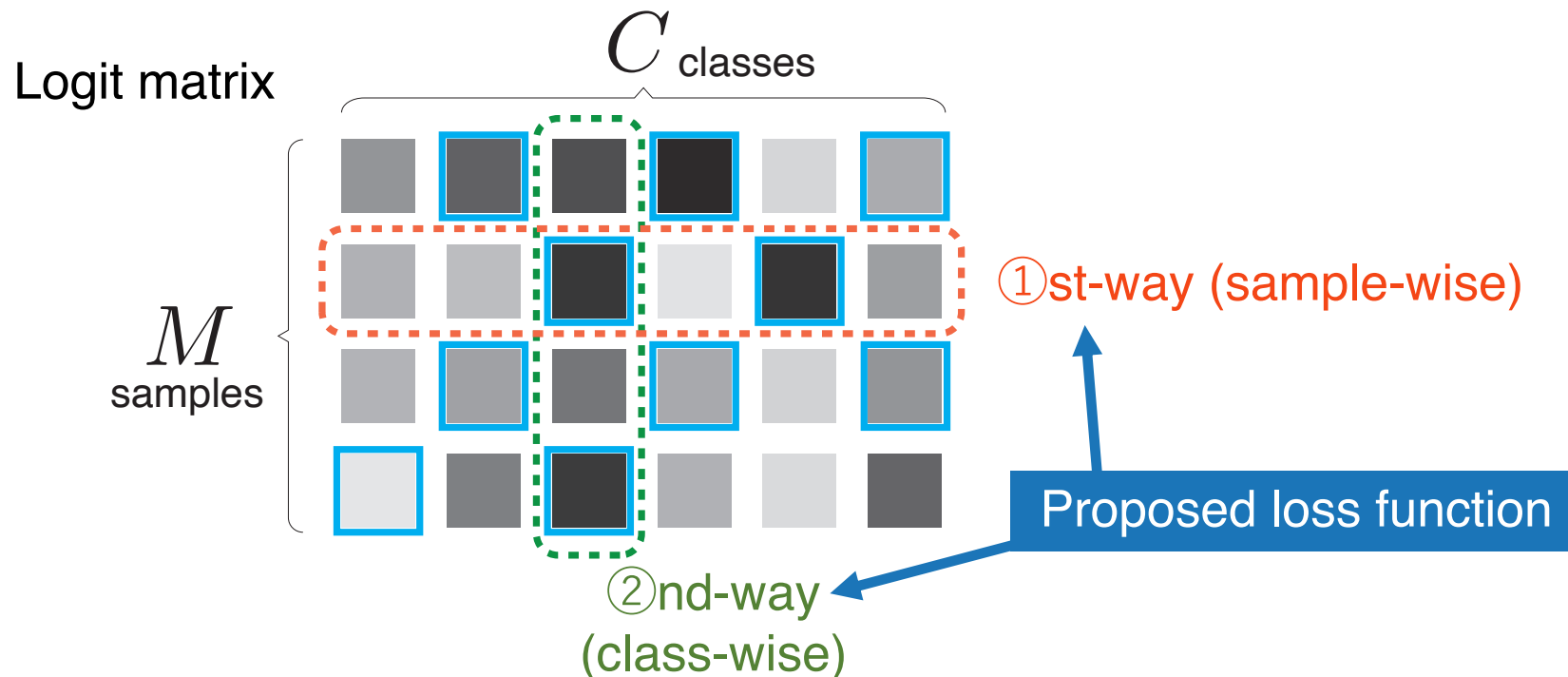
bunch of single-class classification

good at dealing with multiple classes



# Contributions

- We propose a softmax-based multi-label loss function and a novel two-way approach to apply it for learning models.
- The method inherits favorable properties of softmax loss and enhance discriminative power of feature representation from two aspects.



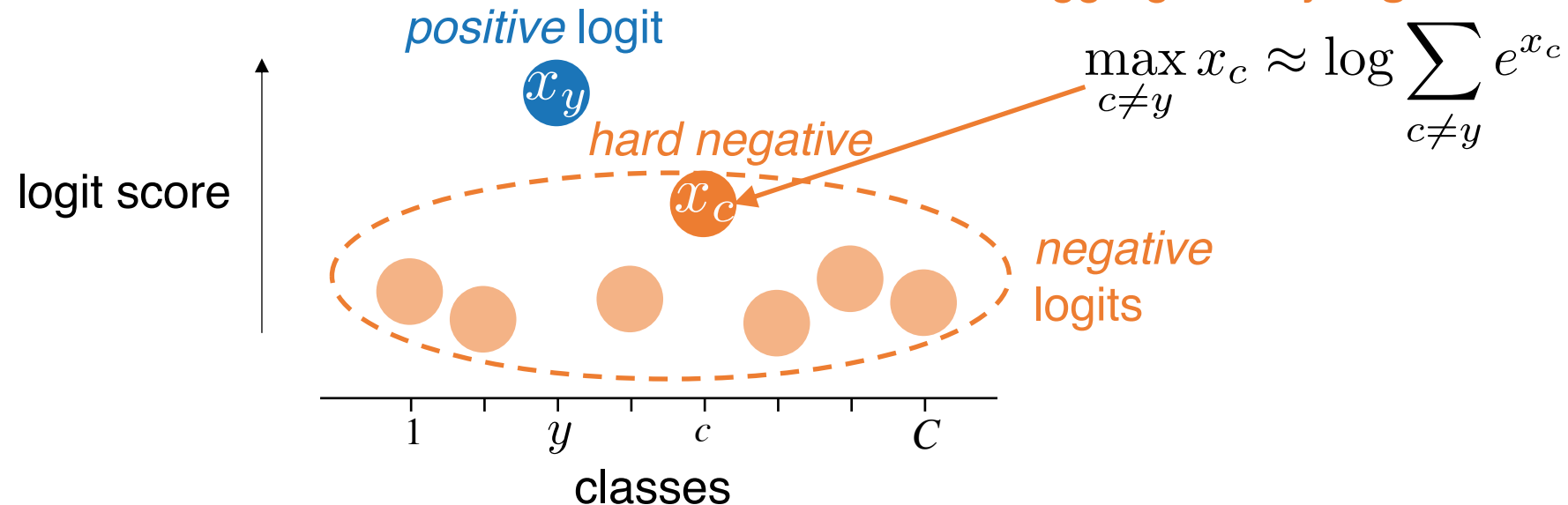
# Revisit: Softmax Loss

- Measure discrepancy between **single ground-truth logit** and **others**.

$$l_{\text{sm}} = -\mathbf{p}_y \log \mathbf{q}(\mathbf{x}) = -\log \frac{e^{x_y}}{\sum_c e^{x_c}} = \text{softplus} \left[ \log \left\{ \sum_{c \neq y} e^{x_c} \right\} - x_y \right]$$

- Find hard negatives.

The other logits are well aggregated by **log-sum-exp**.



# Softmax Loss in Multi-Label Setting

- A straight-forward extension to multiple labels.
  - Average of single softmax losses over given labels.

$$l_{\text{sm}} = -\mathbf{p} \log \mathbf{q}(\mathbf{x}) = \frac{1}{m} \sum_{p=1}^m -\log \frac{e^{x_{y_p}}}{\sum_c e^{x_c}}$$

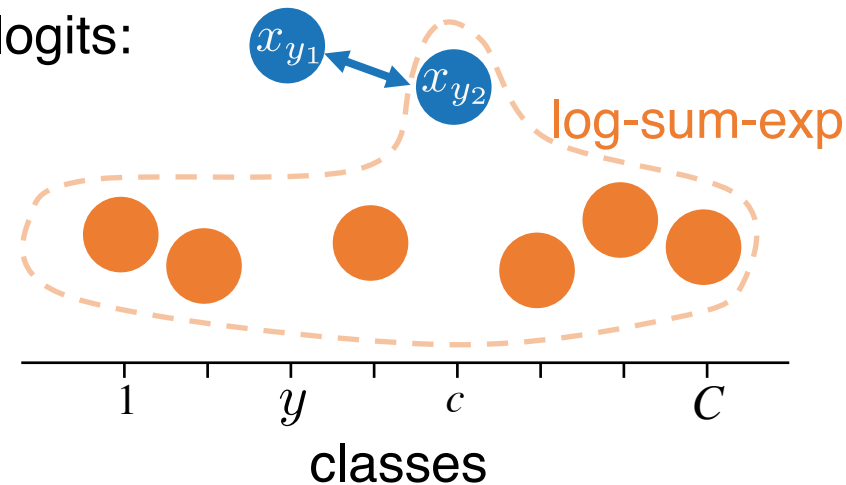
- Positive logits *unfavorably* conflict with each other.

softmax:

$$-\log \frac{e^{x_{y_1}} + e^{x_{y_2}} + \sum_{c \notin \{y_1, y_2\}} e^{x_c}}{e^{x_{y_1}} + e^{x_{y_2}} + \sum_{c \notin \{y_1, y_2\}} e^{x_c}}$$

Annotations: *positive for  $y_1$*  (pointing to  $e^{x_{y_1}}$ ), *positive for  $y_2$*  (pointing to  $e^{x_{y_2}}$ )

logits:



# Multi-label Loss Function

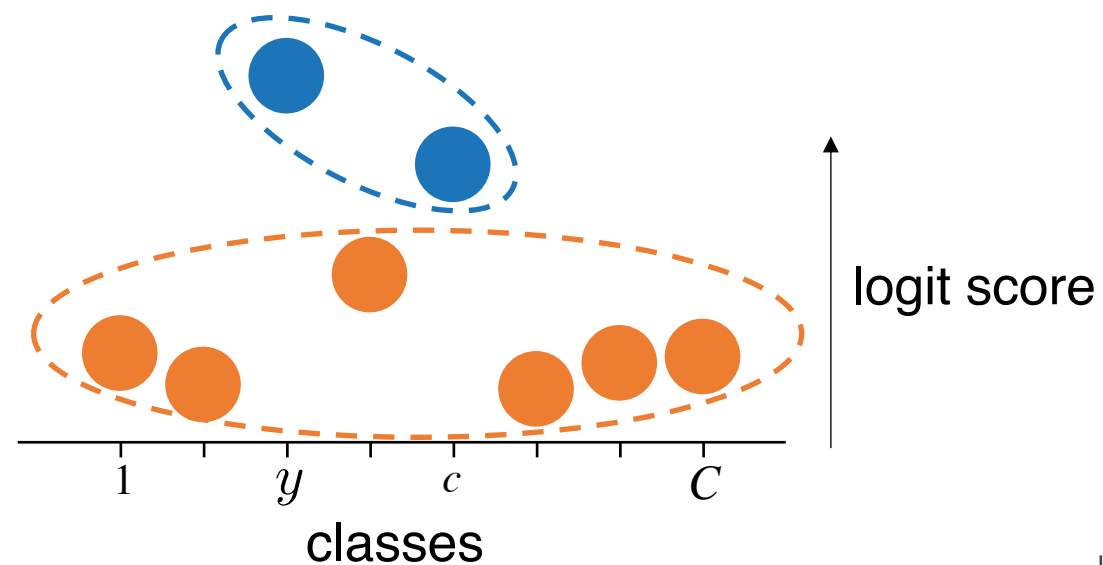
- We derive a novel multi-label loss in a softmax formulation.

$$\ell = \text{softplus} \left[ T_{\mathcal{N}} \log \sum_{n \in \mathcal{N}} e^{\frac{x_n}{T_{\mathcal{N}}}} + T_{\mathcal{P}} \log \sum_{p \in \mathcal{P}} e^{-\frac{x_p}{T_{\mathcal{P}}}} \right]$$

# Multi-label Loss Function

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$$\ell = \text{softplus} \left[ \underbrace{T_{\mathcal{N}} \log \sum_{n \in \mathcal{N}} e^{\frac{x_n}{T_{\mathcal{N}}}}}_{\text{Negative logits}} + \underbrace{T_{\mathcal{P}} \log \sum_{p \in \mathcal{P}} e^{-\frac{x_p}{T_{\mathcal{P}}}}}_{\text{Positive logits}} \right]$$





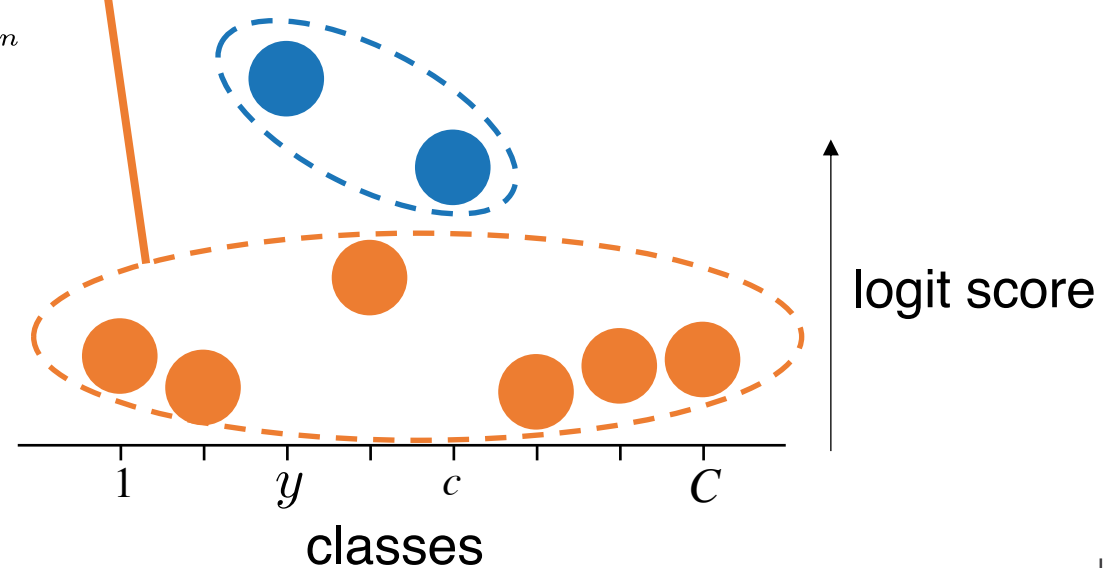
# Multi-label loss function

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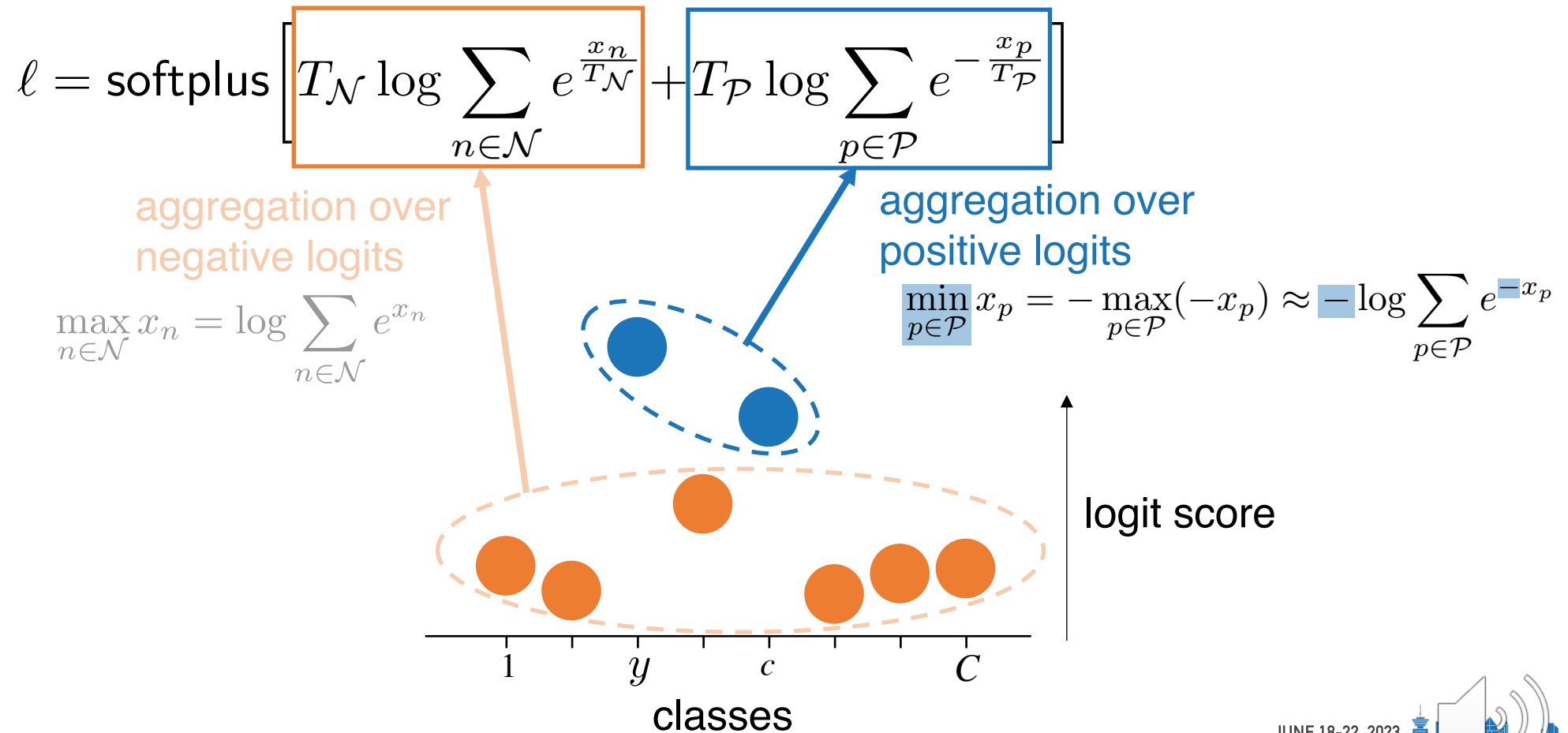
aggregation over  
negative logits

$$\max_{n \in \mathcal{N}} x_n = \log \sum_{n \in \mathcal{N}} e^{x_n}$$



# Multi-label loss function

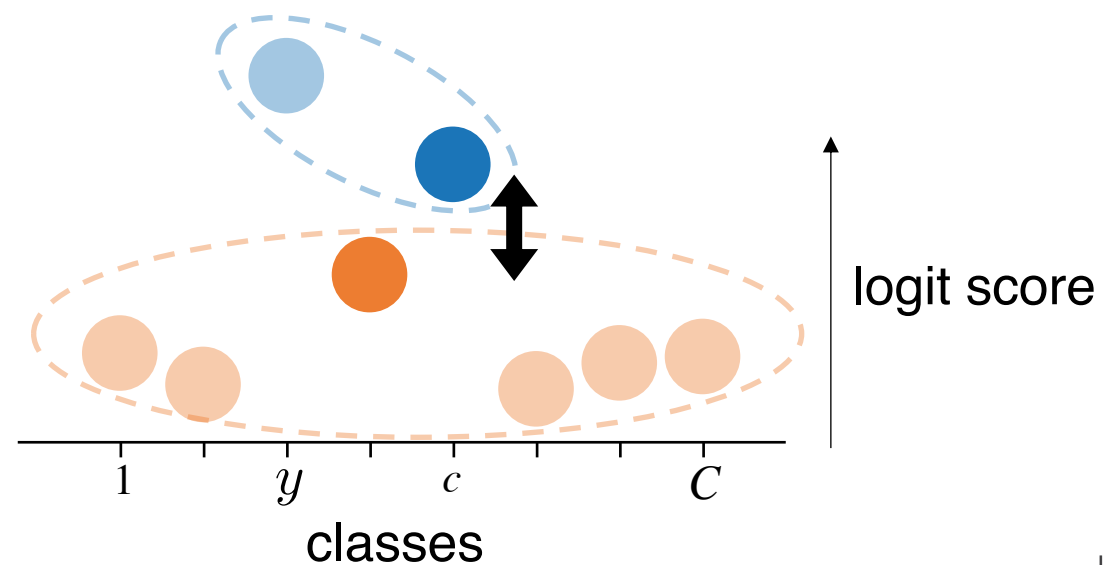
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# Multi-label loss function

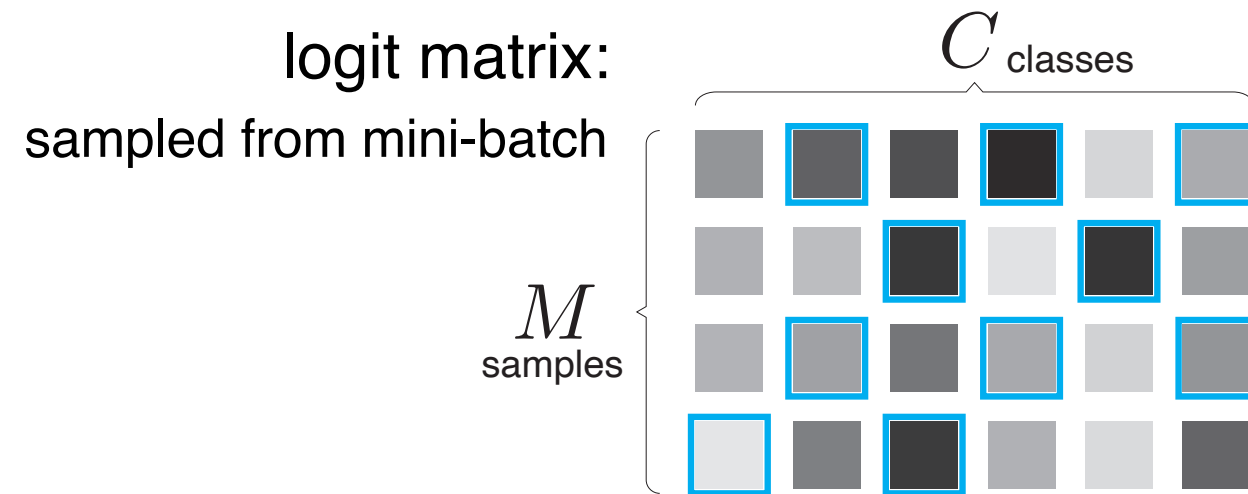
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# Two-way Formulation

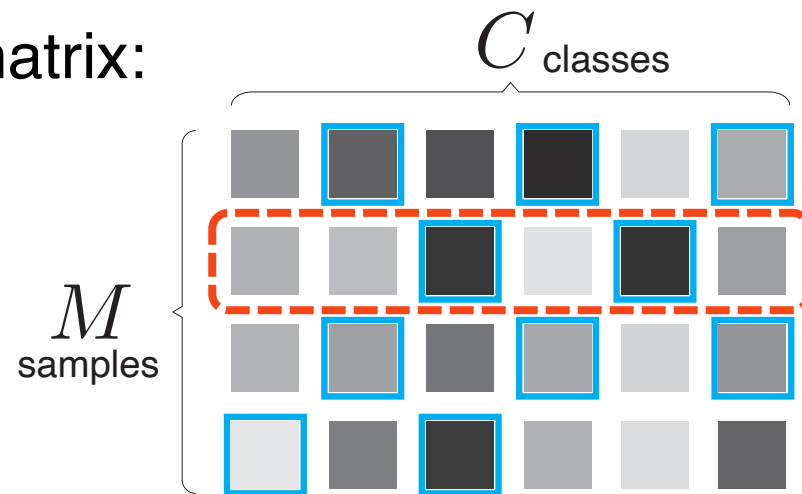
- The multi-label loss function is applied in a **Two-Way** manner.



# Two-way Formulation

- The multi-label loss function is applied in a **Two-Way** manner.

logit matrix:



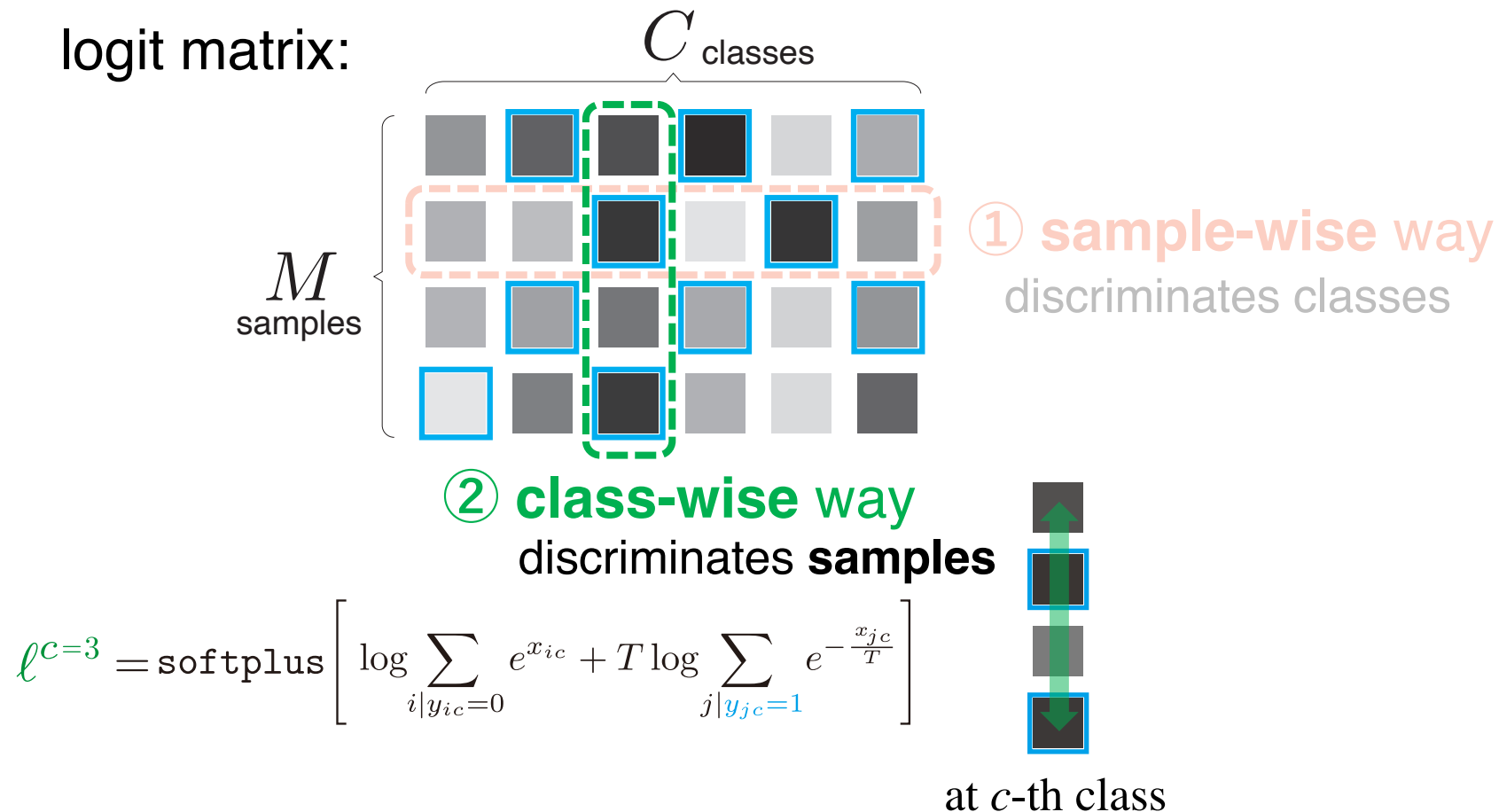
① **sample-wise way**  
discriminates **classes**



$$l_{i=2} = \text{softplus} \left[ \log \sum_{n|y_{in}=0} e^{x_{in}} + T \log \sum_{p|y_{ip}=1} e^{-\frac{x_{ip}}{T}} \right]$$

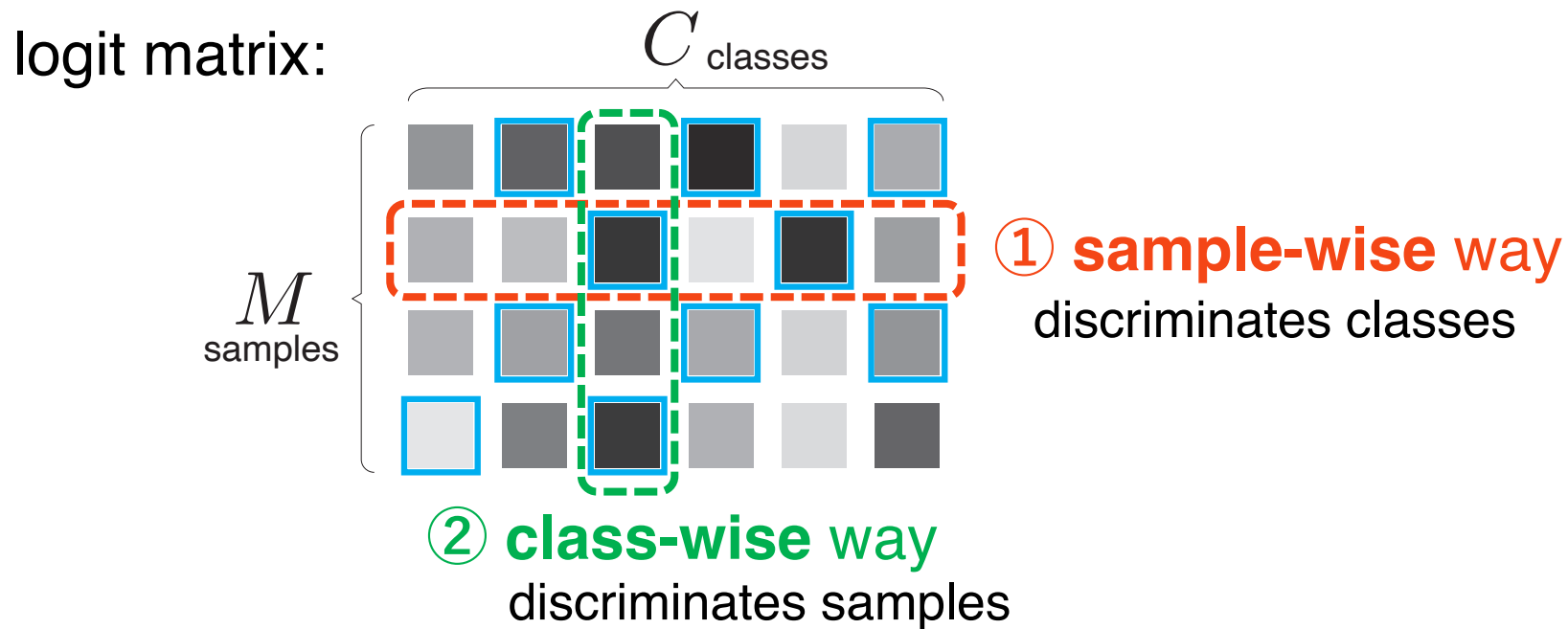
# Two-way Formulation

- The multi-label loss function is applied in a **Two-Way** manner.



# Two-way Formulation

- The multi-label loss function is applied in a **Two-Way** manner.



**Two-way loss:** 
$$\bar{\ell} = \frac{1}{M} \sum_i \ell_i + \frac{1}{C} \sum_c \ell^c$$

# Experimental Results

- Ablation Study: **Ways**

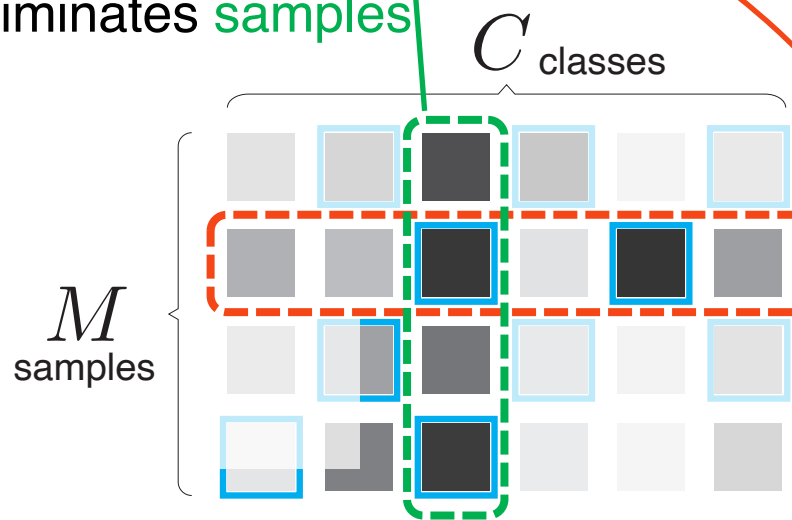
		(a) Ours		(b) Softmax			
	way	both	class	sample	both	class	sample
mAP@class		<b>74.11</b>	<u>73.06</u>	67.18	<b>69.19</b>	<u>68.13</u>	58.00
mAP@sample		<b>86.66</b>	<u>82.75</u>	<u>86.07</u>	<b>84.33</b>	<u>69.15</u>	<u>83.60</u>

MS-COCO dataset



- ✓ zebra
- ✓ giraffe
- ✓ car
- ✓ truck

discriminates **samples**



discriminates **classes**



# Experimental Results

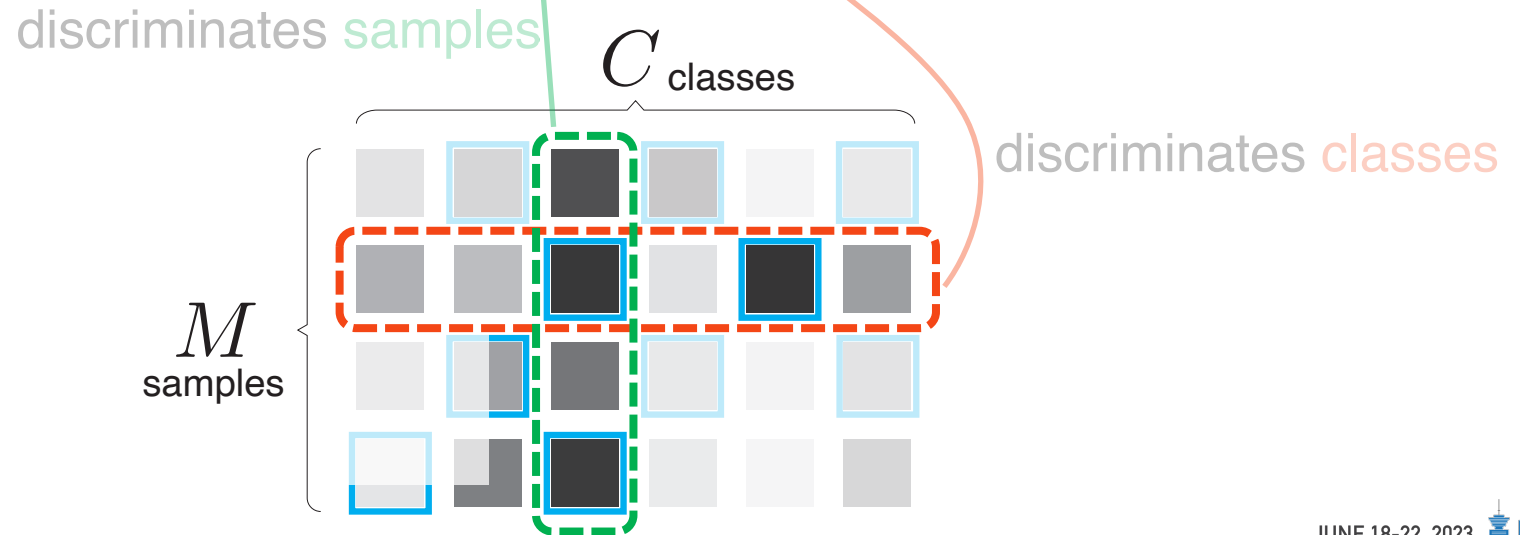
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MS-COCO dataset



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# Experimental Results

- Performance comparison

← various models →

	CNN	mAP@class				mAP@sample			
		ResNet50	ResNeXt50	DenseNet169	RegNetY32gf	ResNet50	ResNeXt50	DenseNet169	RegNetY32gf
<i>MSCOCO</i> [19]	Softmax	58.00	59.53	58.21	64.14	83.60	84.46	83.13	86.92
	BCE	67.71	69.68	64.04	73.38	79.65	80.62	76.14	83.21
	Focal [18]	69.42	71.33	67.18	74.99	84.38	85.22	83.33	87.51
	ASL [2]	70.92	73.04	69.25	76.70	85.05	86.06	84.40	88.29
	Ours	<b>74.11</b>	<b>75.44</b>	<b>73.51</b>	<b>79.57</b>	<b>86.66</b>	<b>87.11</b>	<b>86.62</b>	<b>89.54</b>
<i>VISPR</i> [23]	Softmax	36.61	36.97	28.64	36.79	85.23	<b>85.43</b>	83.75	85.90
	BCE	44.22	45.34	39.73	46.11	72.39	73.14	69.31	73.75
	Focal [18]	46.89	47.76	40.78	48.75	84.35	84.26	82.91	85.29
	ASL [2]	48.53	49.53	42.61	51.03	84.81	84.99	83.99	86.15
	Ours	<b>51.89</b>	<b>52.79</b>	<b>48.57</b>	<b>53.75</b>	<b>85.64</b>	85.40	<b>85.88</b>	<b>86.67</b>
<i>VAW</i> [25]	Softmax	52.59	53.33	47.30	55.02	77.68	78.09	75.97	78.99
	BCE	51.21	51.31	44.53	52.25	72.43	72.29	66.50	72.43
	Focal [18]	54.38	54.50	48.94	56.77	77.66	77.70	75.81	78.71
	ASL [2]	55.39	55.72	48.17	57.88	78.05	78.32	75.91	79.03
	Ours	<b>56.42</b>	<b>57.00</b>	<b>54.28</b>	<b>59.33</b>	<b>78.81</b>	<b>78.95</b>	<b>78.36</b>	<b>80.07</b>
<i>WIDER</i> [17]	Softmax	63.91	65.14	63.61	66.47	83.09	83.74	83.02	84.65
	BCE	70.16	71.40	70.16	73.26	77.62	78.56	77.36	79.94
	Focal [18]	65.88	67.29	64.49	68.72	82.27	82.92	81.89	83.66
	ASL [2]	67.99	69.71	67.34	71.11	83.44	84.12	83.38	85.00
	Ours	<b>72.28</b>	<b>72.77</b>	<b>73.03</b>	<b>74.92</b>	<b>85.43</b>	<b>85.43</b>	<b>85.87</b>	<b>86.97</b>

↑ various datasets ↓

**Thank you !**