

PRDP: Proximal Reward Difference Prediction for Large-Scale Reward Finetuning of Diffusion Models

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A painting of a girl standing on a mountain looking out at an approaching storm over the ocean, with wind blowing and ocean mist, surrounded by lightning.



PRDP Training

Aligning with Human Preferences

- Numerous products

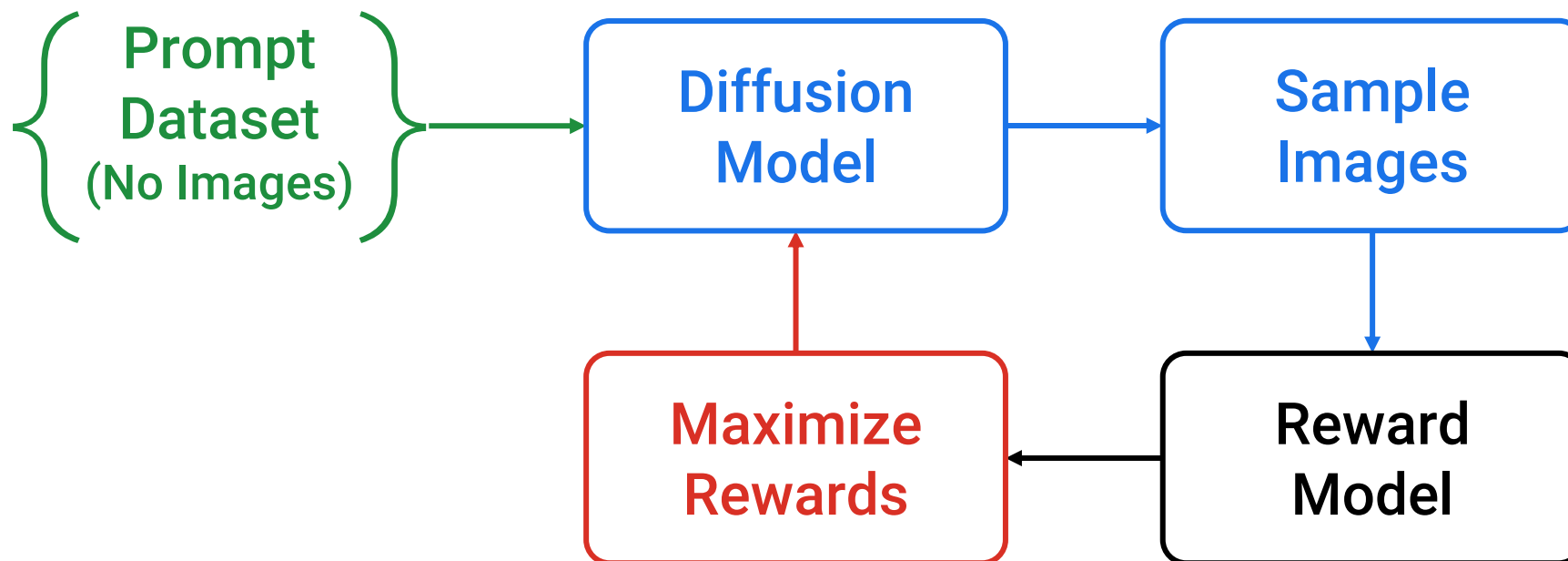


Aligning with Human Preferences

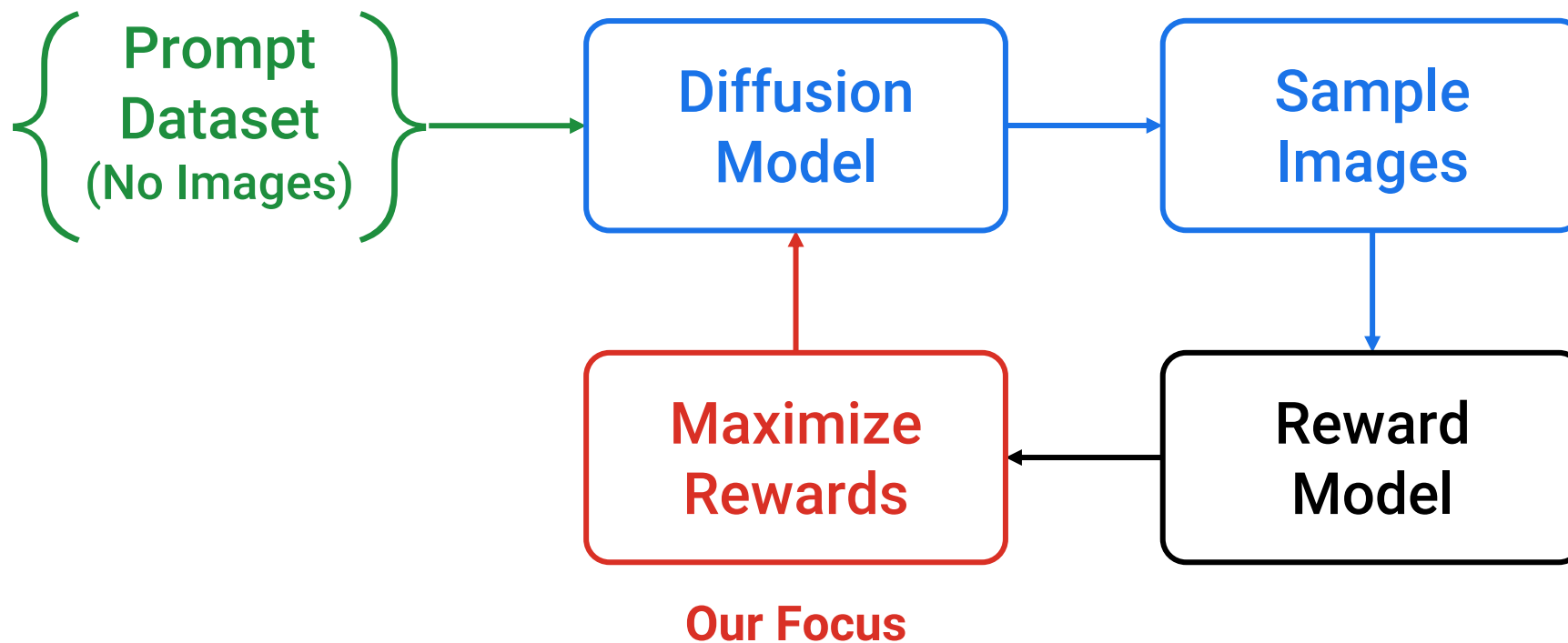
- Our paper



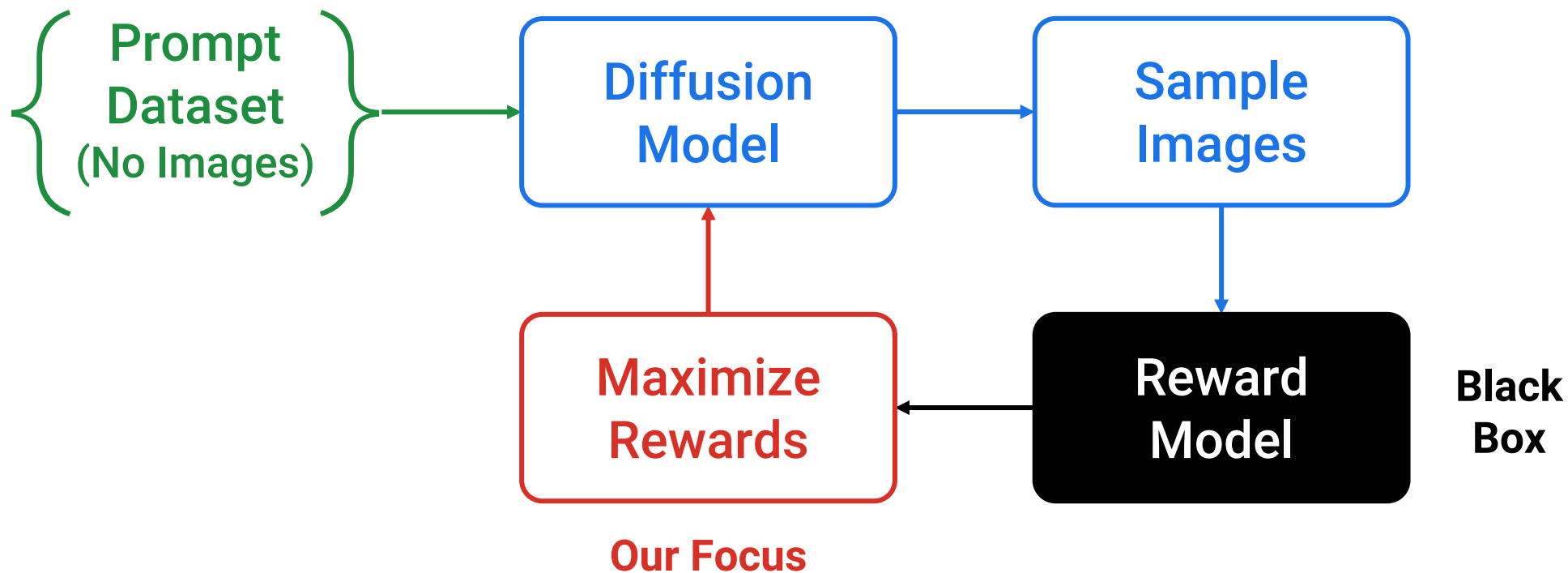
RLHF Pipeline



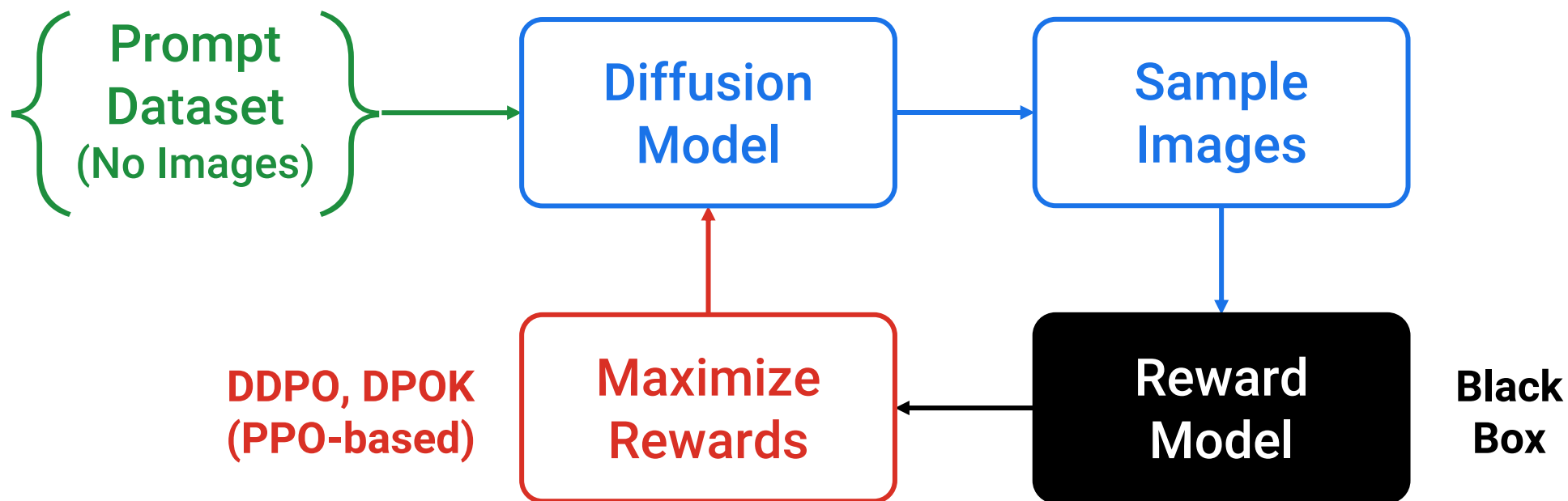
RLHF Pipeline



RLHF Pipeline



RLHF Pipeline

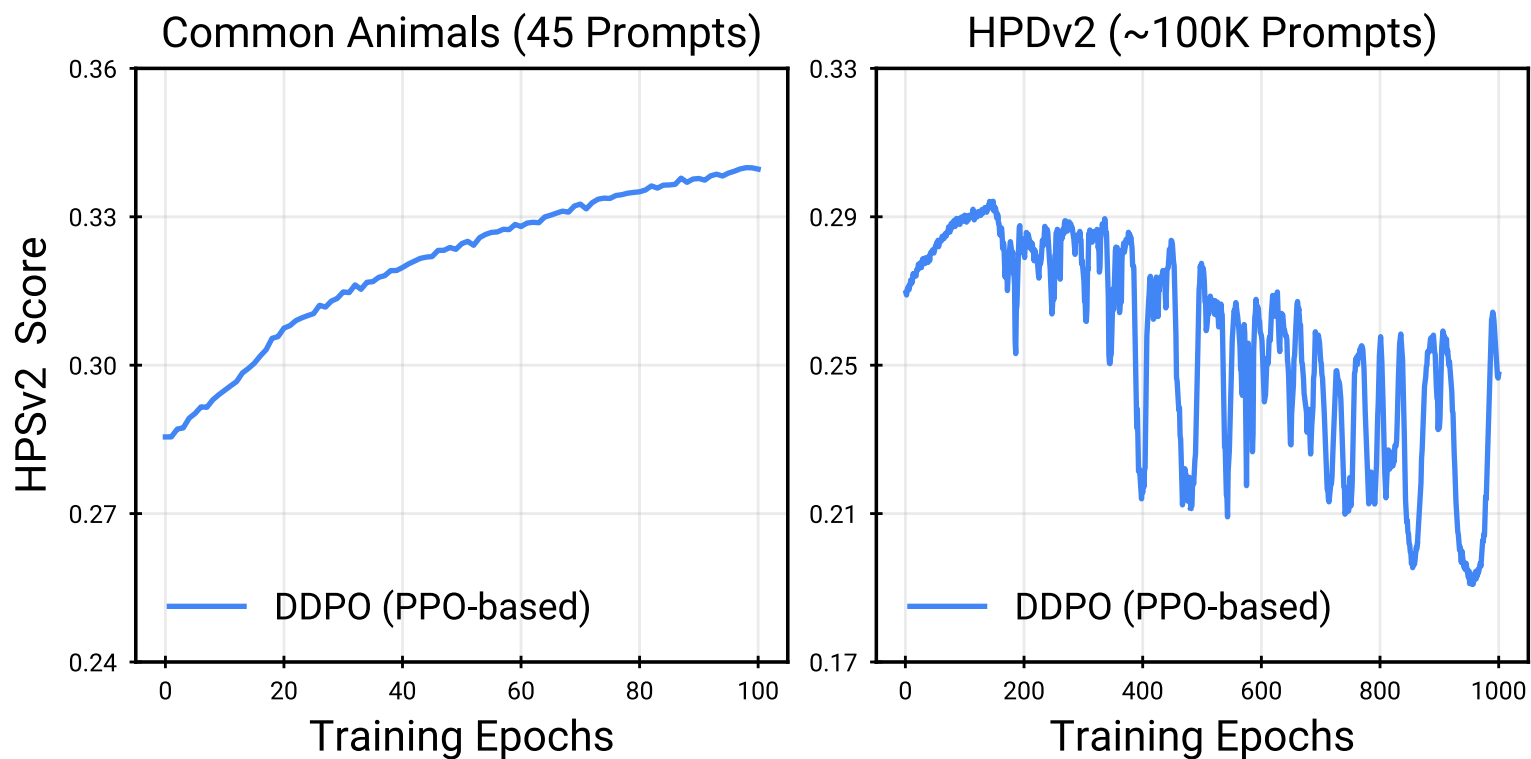


Black *et al.* Training Diffusion Models with Reinforcement Learning. *ICLR 2024*.

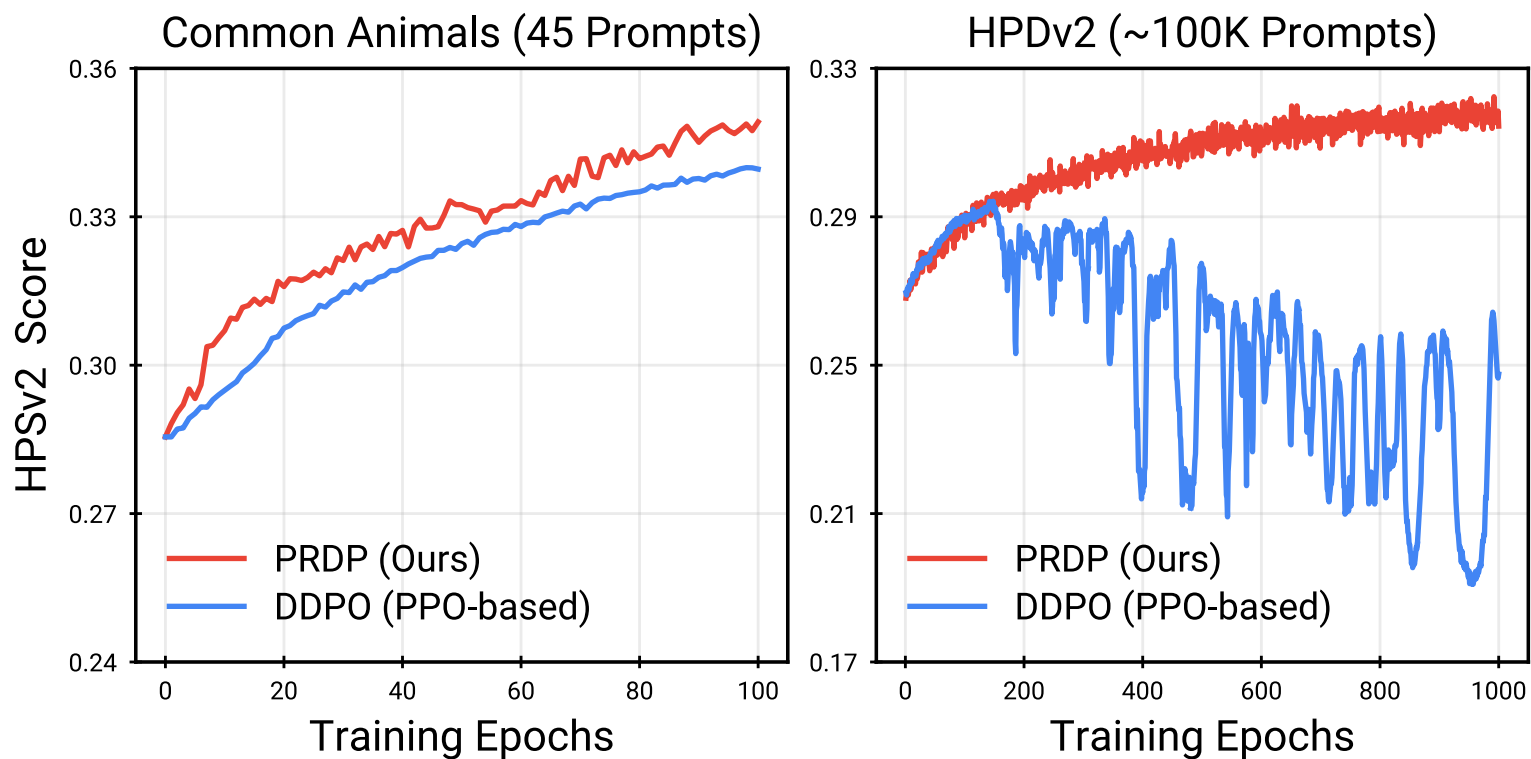
Fan *et al.* DPOK: Reinforcement Learning for Fine-tuning Text-to-Image Diffusion Models. *NeurIPS 2023*.

Schulman *et al.* Proximal Policy Optimization Algorithms.

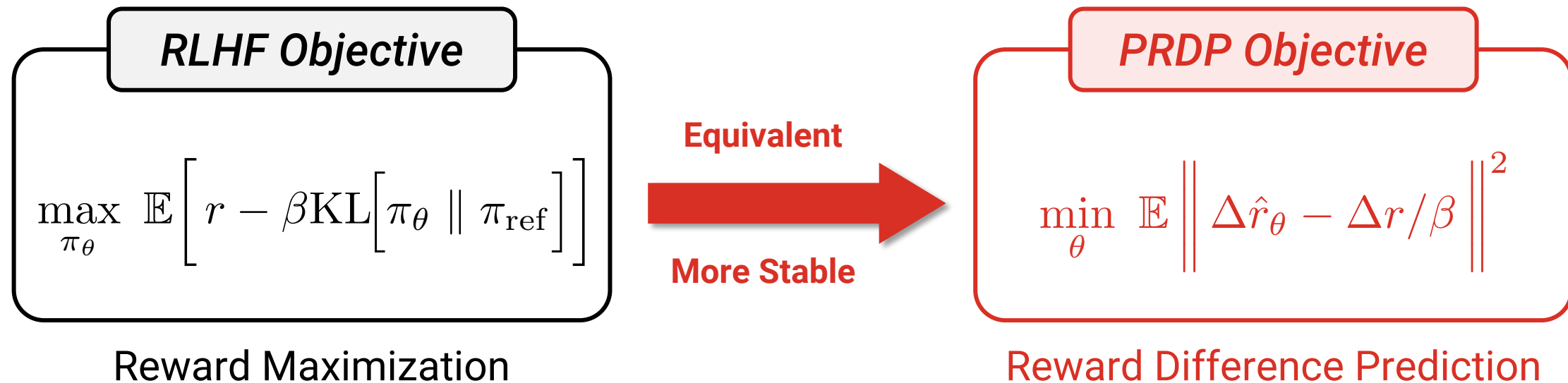
Previous Methods: Unstable at Large Scale



Our Contribution: Stable Large-Scale Training



Method Overview: Novel Training Objective



RLHF Objective

$$\pi_{\theta^*} = \arg \max_{\pi_{\theta}} \mathbb{E}_{\mathbf{c} \sim p(\mathbf{c})} \left[\mathbb{E}_{\mathbf{x}_{0:T} \sim \pi_{\theta}(\mathbf{x}_{0:T} | \mathbf{c})} \left[\underbrace{r(\mathbf{x}_0, \mathbf{c})}_{\text{Reward}} \right] - \beta \text{KL} \left[\underbrace{\pi_{\theta}(\mathbf{x}_{0:T} | \mathbf{c})}_{\text{Diffusion Model}} \parallel \underbrace{\pi_{\text{ref}}(\mathbf{x}_{0:T} | \mathbf{c})}_{\text{Pretrained Diffusion Model}} \right] \right]$$

Labels in the diagram:
 - π_{θ} : Diffusion Model (red)
 - $p(\mathbf{c})$: Prompt Dataset (blue)
 - $\mathbf{x}_{0:T} \sim \pi_{\theta}(\mathbf{x}_{0:T} | \mathbf{c})$: Diffusion Model (red)
 - $r(\mathbf{x}_0, \mathbf{c})$: Reward (blue)
 - $\pi_{\theta}(\mathbf{x}_{0:T} | \mathbf{c})$: Diffusion Model (red)
 - $\pi_{\text{ref}}(\mathbf{x}_{0:T} | \mathbf{c})$: Pretrained Diffusion Model (blue)

Optimal Solution

$$\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c}) = \frac{1}{\underline{Z(\mathbf{c})}} \pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c}) \exp\left(\frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c})\right)$$

Intractable

Optimal Solution

$$\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c}) = \frac{1}{\underline{Z(\mathbf{c})}} \pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c}) \exp\left(\frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c})\right)$$

Intractable



Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c})} = \frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c}) - \log Z(\mathbf{c})$$

Optimal Solution

$$\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c}) = \frac{1}{\underline{Z(\mathbf{c})}} \pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c}) \exp\left(\frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c})\right)$$

Intractable



Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c})} = \frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c}) - \log Z(\mathbf{c})$$

Cancel logZ by considering two denoising trajectories

Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T} | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T} | \mathbf{c})} = \frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c}) - \log Z(\mathbf{c})$$

Cancel logZ by considering two denoising trajectories



Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^a | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^a | \mathbf{c})} - \log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^b | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^b | \mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$

Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^a | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^a | \mathbf{c})} - \log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^b | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^b | \mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$



$$\hat{r}_{\theta}(\mathbf{x}_{0:T}, \mathbf{c}) := \log \frac{\pi_{\theta}(\mathbf{x}_{0:T} | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T} | \mathbf{c})}$$

Equivalent Condition

$$\underline{\hat{r}_{\theta^*}(\mathbf{x}_{0:T}^a, \mathbf{c}) - \hat{r}_{\theta^*}(\mathbf{x}_{0:T}^b, \mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$

Reward Difference Prediction

Equivalent Condition

$$\underline{\hat{r}_{\theta^*}(\mathbf{x}_{0:T}^a, \mathbf{c}) - \hat{r}_{\theta^*}(\mathbf{x}_{0:T}^b, \mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$

Reward Difference Prediction

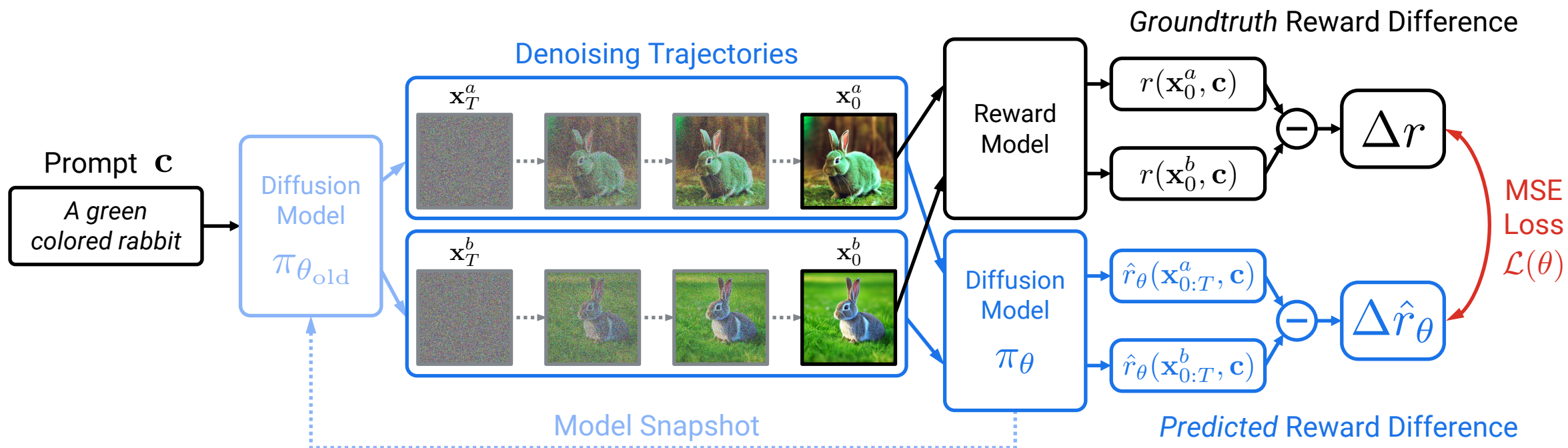


$$\pi_{\theta} = \pi_{\theta^*} \iff \mathcal{L}(\theta) = 0$$

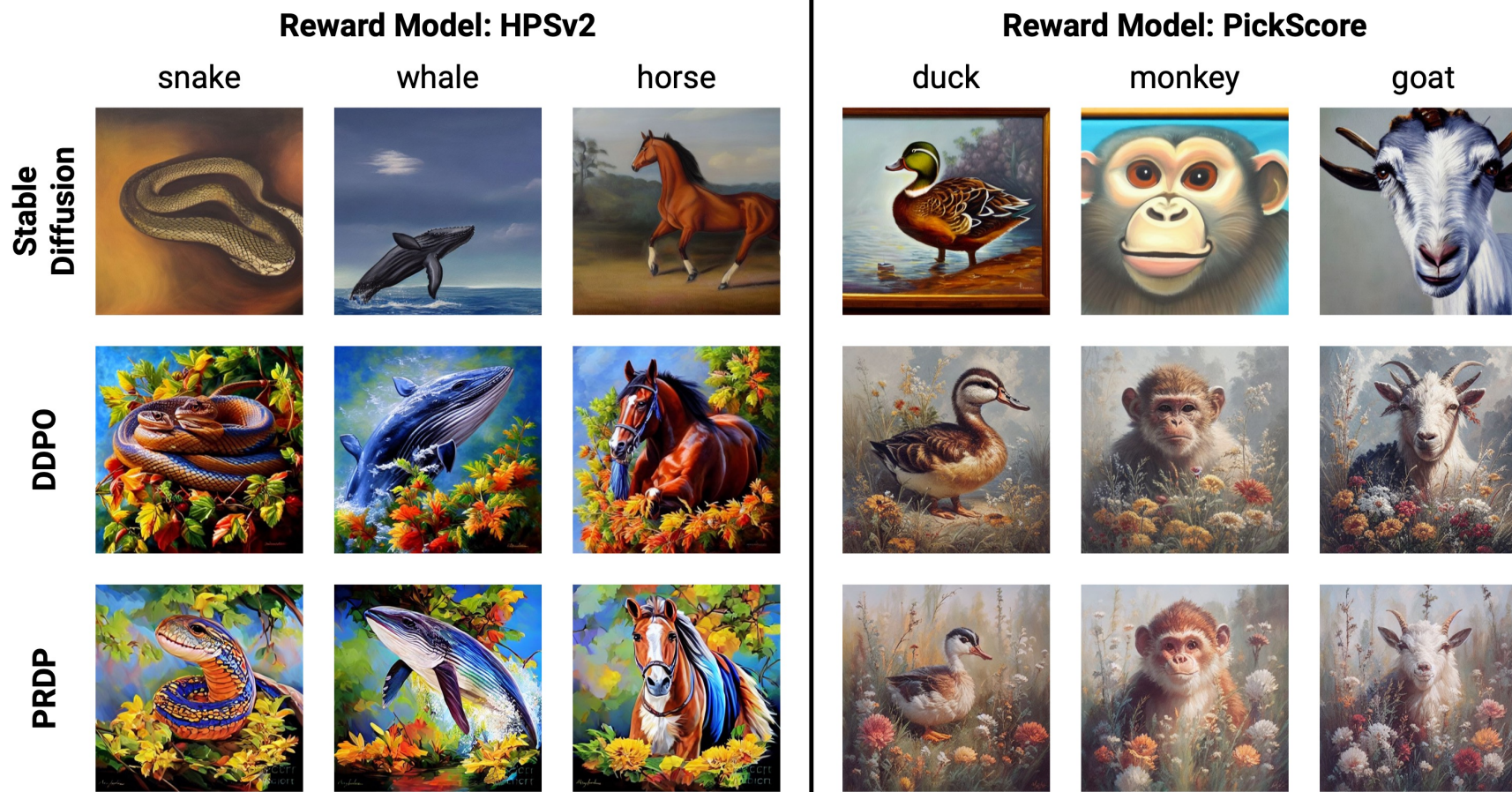
PRDP Objective

$$\mathcal{L}(\theta) = \mathbb{E}_{\mathbf{x}_{0:T}^a, \mathbf{x}_{0:T}^b, \mathbf{c}} \left\| \begin{array}{l} \text{Predicted Reward Difference} \\ \underline{\hat{r}_{\theta}(\mathbf{x}_{0:T}^a, \mathbf{c}) - \hat{r}_{\theta}(\mathbf{x}_{0:T}^b, \mathbf{c})} \\ \text{Groundtruth Reward Difference} \\ - \underline{[r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})] / \beta} \end{array} \right\|^2$$

Online Training Pipeline



Small-Scale Training (45 Prompts)



Wu et al. Human Preference Score v2: A Solid Benchmark for Evaluating Human Preferences of Text-to-Image Synthesis. KIRSTAIN et al. Pick-a-Pic: An Open Dataset of User Preferences for Text-to-Image Generation. *NeurIPS 2023*.

Large-Scale Training (~100K Prompts)

Reward Model: HPSv2

Reward Model: PickScore

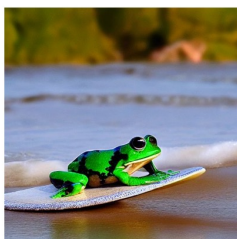
Stable
Diffusion



cinematic still of highly reflective stainless steel train in the desert, at sunset



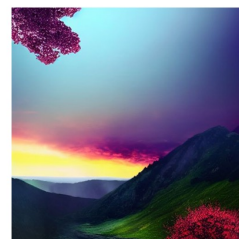
The image is a wooden sculpture of a cute robot with cat ears, displayed in a contemporary art gallery.



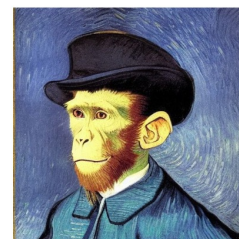
A chibi frog character surfing at the beach.



An anthropomorphic frog wizard wearing a cape and holding a wand.

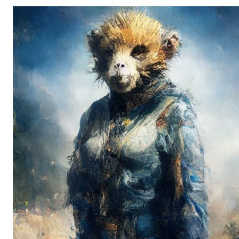
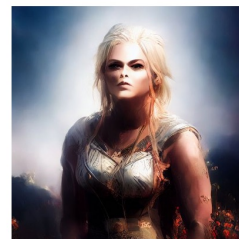
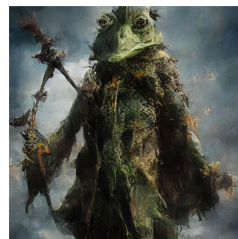
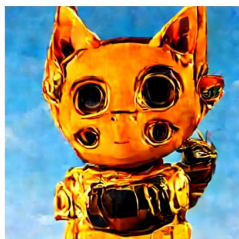
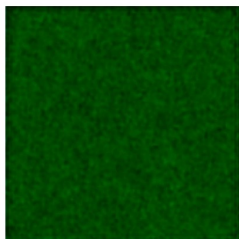


Digital art of a cherry tree overlooking a valley with a waterfall at sunset.



A monkey in a blue top hat painted in oil by Vincent van Gogh in the 1800s.

DDPO

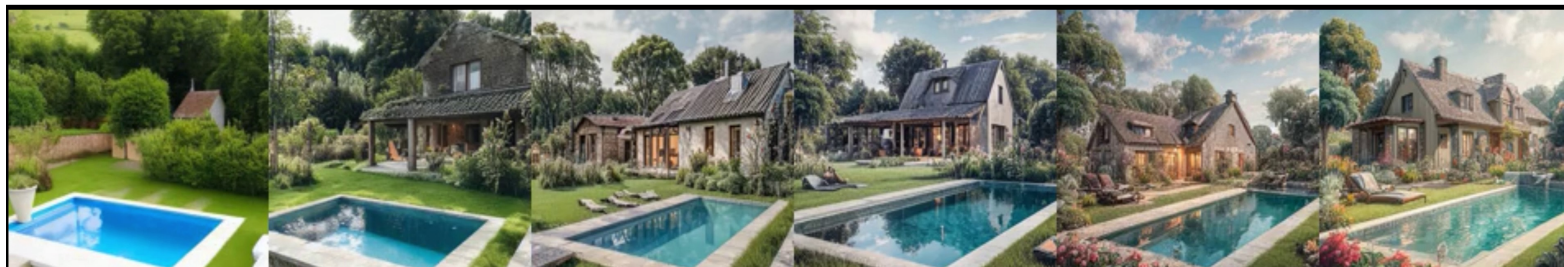


PRDP



Steady Improvement in Large-Scale Training

rural house with a garden and a swimming pool



cinematic still of an adorable walking robot in the desert, at sunset



PRDP Training →

Summary

- PRDP: Scalable diffusion model alignment
- Superior generation quality
- Generalization to unseen prompts

[Project Page](#)



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