# Learning for Transductive Threshold Calibration in Open-World Recognition















Qin Zhang

Dongsheng An Tianjun Xiao

Tong He

Qingming Tang

Tang Y

Ying Nian Wu

Joseph Tighe

Yifan Xing









## **Open-World Recognition (OWR)**

Modern <u>Open-World Recognition (OWR)</u> systems typically use Deep Metric Learning to learn to transform raw data into vectorized representations, where distances between the representations reflect semantic similarities. During testing, the learned model is applied to unseen open-world classes (not encountered during training), with the expectation that similar items still remain close while dissimilar ones will be kept apart.





#### A few notes:

- The classes in  $D_{train}$  and  $D_{test}$  are disjoint.
- Even for the closed-world classes in D<sub>train</sub>, the learned embedding model can exhibit significant variation in intra-class compactness and inter-class separations.
- When applied to the open-world classes in D<sub>test</sub>, this variation in representation structures tends to become more severe.

### **Open-world Threshold Calibration**

- Problem Definition: Open-world calibration <u>amounts to choosing appropriate thresholds of open-world classes</u> (e.g., wolf, sheep, mouse) for an embedding model trained on closed-set classes (dog, cat, bird) <u>to balance the</u> <u>trade-off between TPR and TNR</u>, considering potential distribution shifts and uncertainties in the open world.
- Mathematical formulations Let d and α be the distance threshold and minimum requirement for TPR<sub>test</sub>, we formulate it as a constrained optimization problem:



maximize TNR<sub>test</sub>, subject to TPR<sub>test</sub> $(d) \geq \alpha$ 

### **Limitations of Existing Methods**

- **Problems of existing methods:** Traditional calibration methods like *Platt Scaling and Isotonic Regression* are inductive, relying on a calibration dataset to learn general calibration rules under the assumption of identically distributed data. This assumption often fails in open-world scenarios, where the test distribution is unknown and dynamic, and the calibration dataset may not accurately represent the test data.
- **Our remedial solution** Transductive Threshold Calibration (TTC).



### **OpenGCN: Learning for Transductive Calibration**

- Main Design Concepts:
  - Incorporate TTC by directly predicting the connectivity  $p_{ij}$  between data pairs using a Graph Neural Network (GNN), which can be used for predicting TPR and TNR for the test data at each distance threshold.

$$\mathbf{T}\hat{\mathbf{P}}\mathbf{R}_{\mathsf{test}}(d) = \sum_{i,j\in D_{\mathsf{test}}} \mathbf{1}_{p_{ij}>\tau} \cdot \mathbf{1}_{d_{ij}< d} \Big/ \sum_{i,j\in D_{\mathsf{test}}} \mathbf{1}_{p_{ij}>\tau} \qquad \mathbf{T}\hat{\mathbf{N}}\mathbf{R}_{\mathsf{test}}(d) = \sum_{i,j\in D_{\mathsf{test}}} \mathbf{1}_{p_{ij}\leq\tau} \cdot \mathbf{1}_{d_{ij}>d} \Big/ \sum_{i,j\in D_{\mathsf{test}}} \mathbf{1}_{p_{ij}\leq\tau} \cdot \mathbf{1}_{d_{ij}\leq\tau} \cdot \mathbf{1}_{d_{ij}\leq\tau}$$

• Utilize both training data (for the OWR embedding model) and calibration data for calibration purpose, maximizing the rich information contained within the closed-set data.



(a) Pre-training on Closed-World Examples

#### (b) Fine-tuning on Open-World Examples

### **Experiment Results – SameDist Scenario**

- **Experiment settings:** SameDist identical training and testing distributions.
- Datasets: iNaturalist-2018, CUB-200, Cars-196.
- **Evaluation metrics:** Absolute Error in TPR or TNR. We evaluate at multiple target values (TPR=80%, 90% and TNR=80%, 90%) to provide a comprehensive assessment.





 $AE_{TPR} = |TPR(\hat{d}^{opt}) - TPR_{target}|$   $AE_{TNR} = |TNR(\hat{d}^{opt}) - TNR_{target}|$ 

Table 1. Evaluation in the SameDist scenario using pointwise metrics of  $AE_{TPR}$  (optimize for TPR) and  $AE_{TNR}$  (optimize for TNR). The smaller the metric, the better. For each dataset, the best and second best results are marked in Red and Blue, respectively. Shading in the Table: Gray for posthoc calibration baselines, Cyan for clustering baselines, and Blue for our OpenGCN method. *Best viewed in color*.

	Optimize for TPR=80%		Optimize for TPR=90%			Optimize for TNR=80%			Optimize for TNR=90%				
Method	Cars	CUB	Inat	Cars	CUB	Inat	Cars	CUB	Inat	Cars	CUB	Inat	Rank
Platt scaling [37]	1.35%	5.10%	6.08%	0.44%	2.63%	4.63%	2.83%	2.02%	7.54%	2.93%	6.49%	0.92%	6
Beta calibration [24]	1.13%	5.16%	5.51%	0.02%	2.91%	3.26%	2.94%	1.41%	7.57%	2.78%	6.43%	0.93%	5
Isotonic regression [54]	0.82%	5.28%	4.53%	0.90%	2.56%	3.54%	1.94%	1.00%	5.78%	1.26%	4.65%	0.65%	3
Histogram Calibration [53]	0.82%	5.28%	4.53%	0.90%	2.56%	3.54%	1.94%	1.00%	5.78%	1.26%	4.65%	0.65%	4
DBSCAN [13]	43.11%	18.87%	0.45%	34.57%	9.18%	1.85%	4.09%	13.77%	12.90%	1.60%	9.32%	9.32%	7
Hi-LANDER [49]	3.44%	1.36%	10.54%	2.02%	0.93%	7.00%	0.06%	0.38%	2.35%	0.10%	2.20%	0.21%	2
<b>OpenGCN</b> (ours)	0.33%	0.74%	1.59%	0.72%	1.41%	2.37%	0.61%	0.09%	0.74%	0.58%	0.72%	0.10%	1

### **Experiment Results – ShiftDist Scenario**

• Experiment settings: ShiftDist – slightly shifted distributions between training and calibration.

av

• Evaluation metrics: The combined Mean Absolute Error for both TPR and TNR averaged over  $d \in [0,2]$ .

$$MAE_{comb} = \frac{1}{2} \int_0^2 \left( |T\hat{P}R(d) - TPR(d)| + |T\hat{N}R(d) - TNR(d)| \right) dd$$

Table 2. Evaluation on the Cars-196 dataset in the ShiftDist scenario across 13 common corruption and perturbation types using combined global error metric of  $MAE_{comb}$ . The best results are marked in Red.

Noise			Blur			Weather			Digital				
Gauss	Shot	Impulse	Defocus	Motion	Zoom	Snow	Fog	Bright	Contrast	Elastic	Pixel	JPEG	Rank
2.95e-2	2.99e-2	3.41e-2	2.66e-2	2.62e-2	5.02e-2	4.24e-2	4.37e-2	2.16e-2	4.61e-2	2.16e-2	2.24e-2	2.03e-2	4
2.94e-2	2.97e-2	3.41e-2	2.67e-2	2.69e-2	5.06e-2	4.32e-2	4.37e-2	2.18e-2	4.61e-2	2.20e-2	2.23e-2	2.02e-2	5
2.88e-2	2.85e-2	3.38e-2	2.37e-2	2.31e-2	4.85e-2	4.07e-2	4.34e-2	1.83e-2	4.59e-2	1.85e-2	2.03e-2	1.80e-2	2
2.88e-2	2.85e-2	3.38e-2	2.37e-2	2.31e-2	4.85e-2	4.07e-2	4.34e-2	1.83e-2	4.59e-2	1.85e-2	2.03e-2	1.80e-2	3
1.96e-2	6.02e-2	7.79e-2	9.81e-2	1.13e-1	1.22e-1	1.19e-1	4.02e-2	9.27e-2	4.53e-2	1.09e-1	1.04e-1	8.21e-2	7
7.65e-2	6.30e-2	6.59e-2	3.98e-2	5.33e-2	4.48e-2	5.94e-2	7.16e-2	5.09e-2	9.45e-2	4.42e-2	9.48e-2	6.91e-2	6
1.33e-2	5.87e-3	1.66e-2	1.50e-2	1.71e-2	3.92e-2	1.42e-2	7.32e-3	6.73e-3	7.08e-3	5.34e-3	1.15e-2	1.68e-2	1
3.82%	79.40%	50.89%	36.71%	25.97%	12.50%	65.11%	81.79%	63.22%	84.37%	71.14%	43.35%	6.67%	55.03% (avg.)
					Autom	THE							
					Sec. 1								
ot noise	Impulse nois	e Defocus b	lur Motior	ı blur Za	om blur	Snow	Fog	Bright	ness Con	trast Elast	ic transform	Pixelate	JPEG
	Gauss         .95e-2         .94e-2         .88e-2         .96e-2         .65e-2         .33e-2         3.82%	Noise         Sauss       Shot         .95e-2       2.99e-2         .94e-2       2.97e-2         .88e-2       2.85e-2         .88e-2       2.85e-2         .96e-2       6.02e-2         .65e-2       6.30e-2         .33e-2 <b>5.87e-3</b> 3.82% <b>79.40%</b>	Noise           Gauss         Shot         Impulse           .95e-2         2.99e-2         3.41e-2           .94e-2         2.97e-2         3.41e-2           .88e-2         2.85e-2         3.38e-2           .88e-2         2.85e-2         3.38e-2           .96e-2         6.02e-2         7.79e-2           .65e-2         6.30e-2         6.59e-2           .33e-2 <b>5.87e-3 1.66e-2</b> 3.82% <b>79.40% 50.89%</b>	Noise         Impulse         Defocus           95e-2         2.99e-2         3.41e-2         2.66e-2           94e-2         2.97e-2         3.41e-2         2.67e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2           .96e-2         6.02e-2         7.79e-2         9.81e-2           .65e-2         6.30e-2         6.59e-2         3.98e-2           .33e-2         5.87e-3         1.66e-2         1.50e-2           .882%         79.40%         50.89%         36.71%	Noise         Blur           Gauss         Shot         Impulse         Defocus         Motion           .95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2           .94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2           .96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1           .65e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2           .33e-2         5.87e-3         1.66e-2         1.50e-2         1.71e-2           .882%         79.40%         50.89%         36.71%         25.97%	Noise         Blur           Gauss         Shot         Impulse         Defocus         Motion         Zoom           95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2           94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2           .96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1           .65e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2           .33e-2 <b>5.87e-3</b> 1.66e-2         1.50e-2         1.71e-2         3.92e-2           .82%         79.40%         50.89%         36.71%         25.97%         12.50%	Noise         Blur           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow           95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2           94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2           .96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1           .65e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2         5.94e-2           .33e-2         5.87e-3         1.66e-2         1.50e-2         1.71e-2         3.92e-2         1.42e-2           .82%         79.40%         50.89%         36.71%         25.97%         12.50%         65.11%	Noise         Blur         Weather           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow         Fog           .95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2         4.37e-2           .94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2         4.37e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2           .96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1         4.02e-2           .65e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2         5.94e-2         7.16e-2           .33e-2         5.87e-3         1.66e-2         1.50e-2         1.71e-2         3.92e-2         1.42e-2         7.32e-3           .820%         79.40%         50.89%         36.71%         25.97%         12.50%         65.11%         81.79%	Noise         Blur         Weather           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow         Fog         Bright           95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2         4.37e-2         2.16e-2           94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2         4.37e-2         2.18e-2           88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2         1.83e-2           96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1         4.02e-2         9.27e-2           .65e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2         5.94e-2         7.16e-2         5.09e-2           .33e-2         5.87e-3         1.66e-2         1.50e-2         1.71e-2         3.92e-2         1.42e-2         7.32e-3         6.73e-3           3.82%         79.40%         50.89%         36.71%         25.97%         12.50%         65.11%         81.79%         63.22%	Noise         Blur         Weather           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow         Fog         Bright         Contrast           95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2         4.37e-2         2.16e-2         4.61e-2           94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2         4.37e-2         2.18e-2         4.61e-2           88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2         1.83e-2         4.59e-2           96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1         4.02e-2         9.27e-2         4.53e-2           96e-2         6.02e-2         7.79e-2         9.81e-2         1.3e-1         1.22e-1         1.19e-1         4.02e-2         9.27e-2         4.53e-2           96e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2         5.94e-2         7.16e-2         5.09e-2         9.45e-2           33e-2         5.87e-3         1.66e-2         1.50e-2	Noise         Blur         Weather         Digi           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow         Fog         Bright         Contrast         Elastic           95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2         4.37e-2         2.16e-2         4.61e-2         2.16e-2           94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2         4.37e-2         2.18e-2         4.61e-2         2.20e-2           88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2         1.83e-2         4.59e-2         1.85e-2           96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1         4.02e-2         9.27e-2         4.53e-2         1.09e-1           .65e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2         5.94e-2         7.16e-2         5.09e-2         9.45e-2         4.42e-2           .33e-2         5.87e-3         1.66e-2         1.50e-2         1.250%         65.11%         81.79%         63	Noise         Blur         Weather         Digit           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow         Fog         Bright         Contrast         Elastic         Pixel           .95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2         4.37e-2         2.16e-2         4.61e-2         2.16e-2         2.20e-2         2.23e-2           .94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2         4.37e-2         2.18e-2         4.61e-2         2.20e-2         2.23e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2         1.83e-2         4.59e-2         1.85e-2         2.03e-2           .88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         9.27e-2         4.59e-2         1.85e-2         2.03e-2           .96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1         4.02e-2         9.27e-2         4.42e-2         9.48e-2           .33e-2         5.87e-3	Noise         Blur         Weather         Digital           Gauss         Shot         Impulse         Defocus         Motion         Zoom         Snow         Fog         Bright         Contrast         Elastic         Pixel         JPEG           95e-2         2.99e-2         3.41e-2         2.66e-2         2.62e-2         5.02e-2         4.24e-2         4.37e-2         2.16e-2         4.61e-2         2.16e-2         2.24e-2         2.03e-2           94e-2         2.97e-2         3.41e-2         2.67e-2         2.69e-2         5.06e-2         4.32e-2         4.37e-2         2.18e-2         4.61e-2         2.20e-2         2.23e-2         2.02e-2           88e-2         2.85e-2         3.38e-2         2.37e-2         2.31e-2         4.85e-2         4.07e-2         4.34e-2         1.83e-2         4.59e-2         1.85e-2         2.03e-2         1.80e-2           96e-2         6.02e-2         7.79e-2         9.81e-2         1.13e-1         1.22e-1         1.19e-1         4.02e-2         9.27e-2         4.45e-2         9.48e-2         6.99e-2         1.99e-1         1.04e-1         8.21e-2           96e-2         6.30e-2         6.59e-2         3.98e-2         5.33e-2         4.48e-2         5.94e-2

### **Experiment Results – DiffDist Scenario**

- **Experiment settings:** DiffDist significantly different distributions between training and calibration data. In particular, we consider the following:
  - <u>Long-tailed calibration</u>: We divide iNaturalist's test classes into two sets based on cluster size, each containing the same number of images. For calibration, we use the head set (with a more images per class) as the calibration data and the tail set (with fewer images per class) for testing.
  - <u>Out-of-domain calibration</u>:
    - For Cars, we transform its test partition into sketches, while leaving the training and calibration partitions untouched.
    - We also consider cross-dataset calibration, where the OpenGCN model is pretrained and fine-tuned on iNaturalist (general natural species images) but tested on CUB (bird images).
- Evaluation metrics: The combined Mean Absolute Error.

Table 3. Evaluation in the DiffDist scenario using the global error metric  $MAE_{comb}$ . The best results are highlighted in Red.

Method	Cars: Sketch	CUB: Cross-dataset	iNat: Longtail		
Platt scaling	1.08e-1	1.15e-1	2.09e-2		
Beta calibration	1.08e-1	1.15e-1	2.12e-2		
Isotonic regression	1.08e-1	1.15e-1	2.11e-2		
Histogram Calibration	1.08e-1	1.15e-1	2.11e-2		
DBSCAN	5.16e-2	1.60e-1	7.21e-2		
Hi-LANDER	6.67e-2	1.30e-1	6.26e-2		
OpenGCN (ours)	3.54e-2	1.42e-2	1.82e-2		
Imp. over top baseline $\uparrow$	31.40%	87.65%	12.92%		

### Takeaways for "Learning for Transductive Threshold Calibration in Open-World Recognition"



- We formally define the open-world threshold calibration problem for DML-based open-world visual recognition systems, identifying key challenges associated with the task.
- We introduce OpenGCN, a meta learning framework that enables transductive threshold calibration via a GNN. Importantly, OpenGCN does not rely on the assumption of matching distance distributions between the calibration dataset and the test dataset.
- The evaluation results underscore OpenGCN's effectiveness across different distance distribution patterns between the calibration dataset and test dataset, highlighting its practical applicability for threshold calibration in DML-based open-world recognition.
- (Limitations) Compared to traditional calibration methods, OpenGCN is less efficient and more susceptible to over-parameterization. Furthermore, OpenGCN is not a calibration-data-free method as it still requires some calibration data in addition to the closed-world data used for training the embedding model.

For more details, please refer to our paper at <u>https://arxiv.org/html/2305.12039v2</u>!

